



Sensitivity of astrophysical reaction rate to nuclear level density across different energy intervals

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Astrophysics

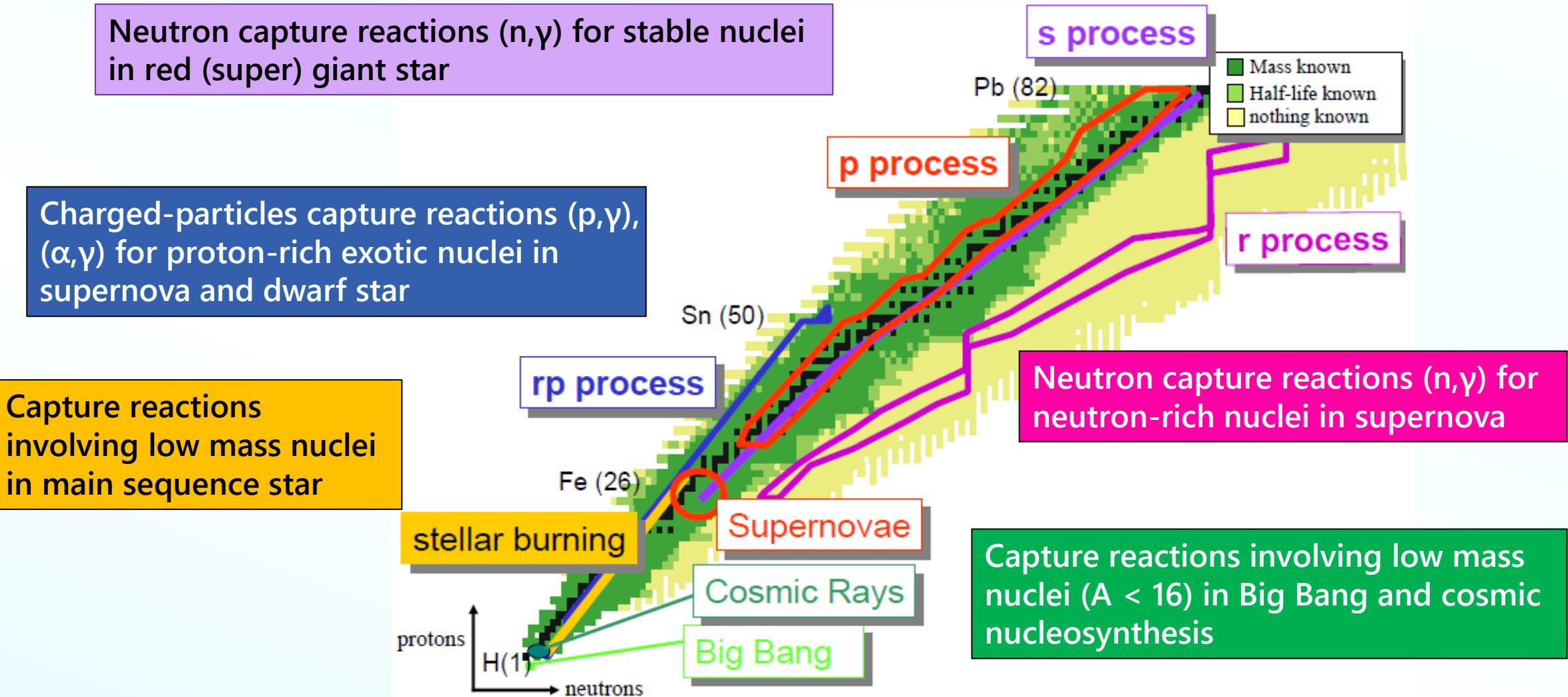


Figure taken from: H Grawe, K Langanke, and G Martinez-Pinedo, Reports on Progress in Physics (2007) 70 9

Reaction model

Hauser-Feshbach formalism of $\sigma_{(a,\gamma)}$

✓ capture reaction $A(a, \gamma)B$

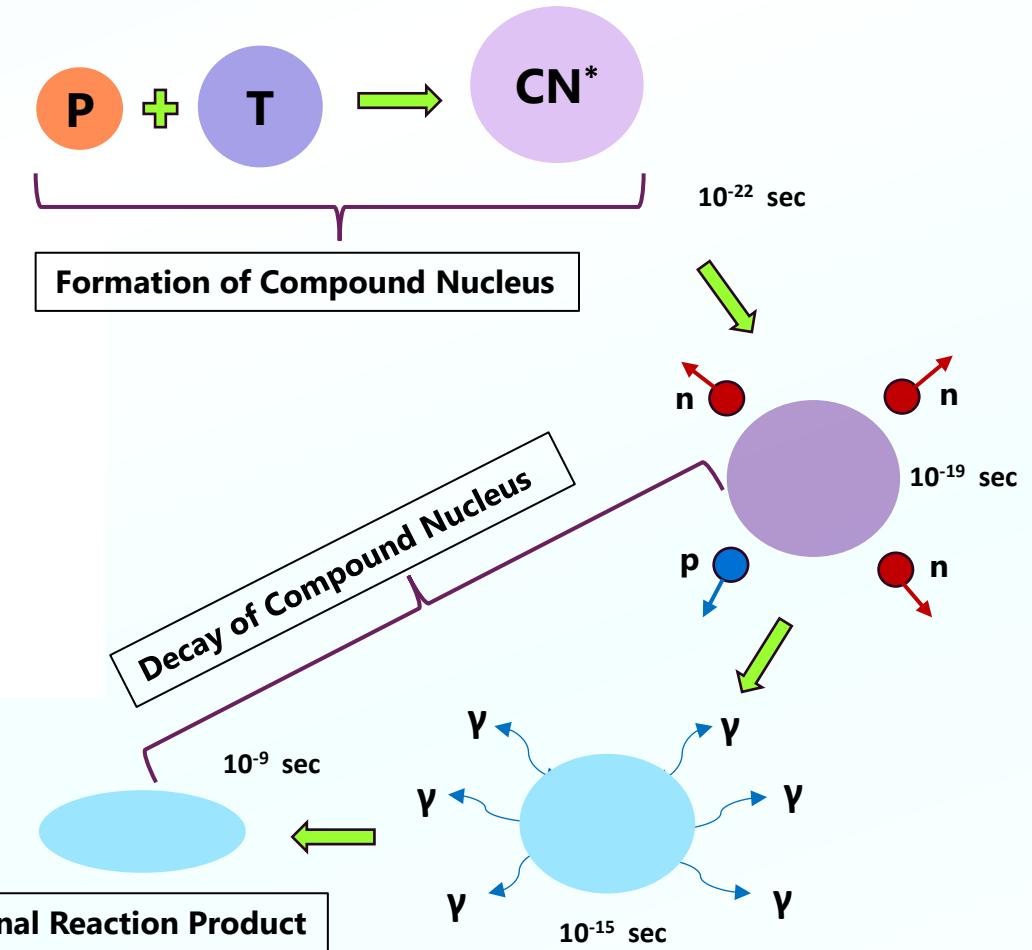
$$\sigma_{A+a \rightarrow B^x + \gamma}^{CNC} = \frac{\pi}{k^2} \sum_{J=mod(I_A+I_a,1)}^{l_{max}+I_A+I_a} \sum_{\Pi=-1}^1 \frac{2J+1}{(2I_A+1)(2I_a+1)} \\ \times \sum_{J_p=|J-J_A|}^{J+I_A} \sum_{l_i=|J_a-I_a|}^{J_a+I_a} \sum_{\lambda=|J-I_B^x|}^{J+I_B^x} \sum_{l_f=|\lambda-I_\gamma|}^{\lambda+I_\gamma} \delta_{C_a}^\pi \delta_{C_\gamma}^\pi \\ \times \frac{\langle T_{C_a, l_i, J_a}^J(E) \rangle \langle T_{C_\gamma, l_f, \lambda}^J(E_\gamma) \rangle}{\sum_{C l j} \delta_C^\pi \langle T_{C, l, j}^J(E_C) \rangle} W_{C_a l_i J_a C_\gamma l_f \lambda}^J$$

❖ uses the nuclear level density (NLD) as an input

$$\rho_t(E_x) = \sum_J \sum_\pi \rho(E_x, J, \Pi)$$

reaction rate

$$N_A \langle \sigma v \rangle = \left(\frac{8}{\pi m_{01}} \right)^{1/2} \frac{N_A}{(kT)^{3/2}} \int_0^\infty E \sigma(E) e^{-E/kT} dE$$



Sensitivity of the reaction cross-section

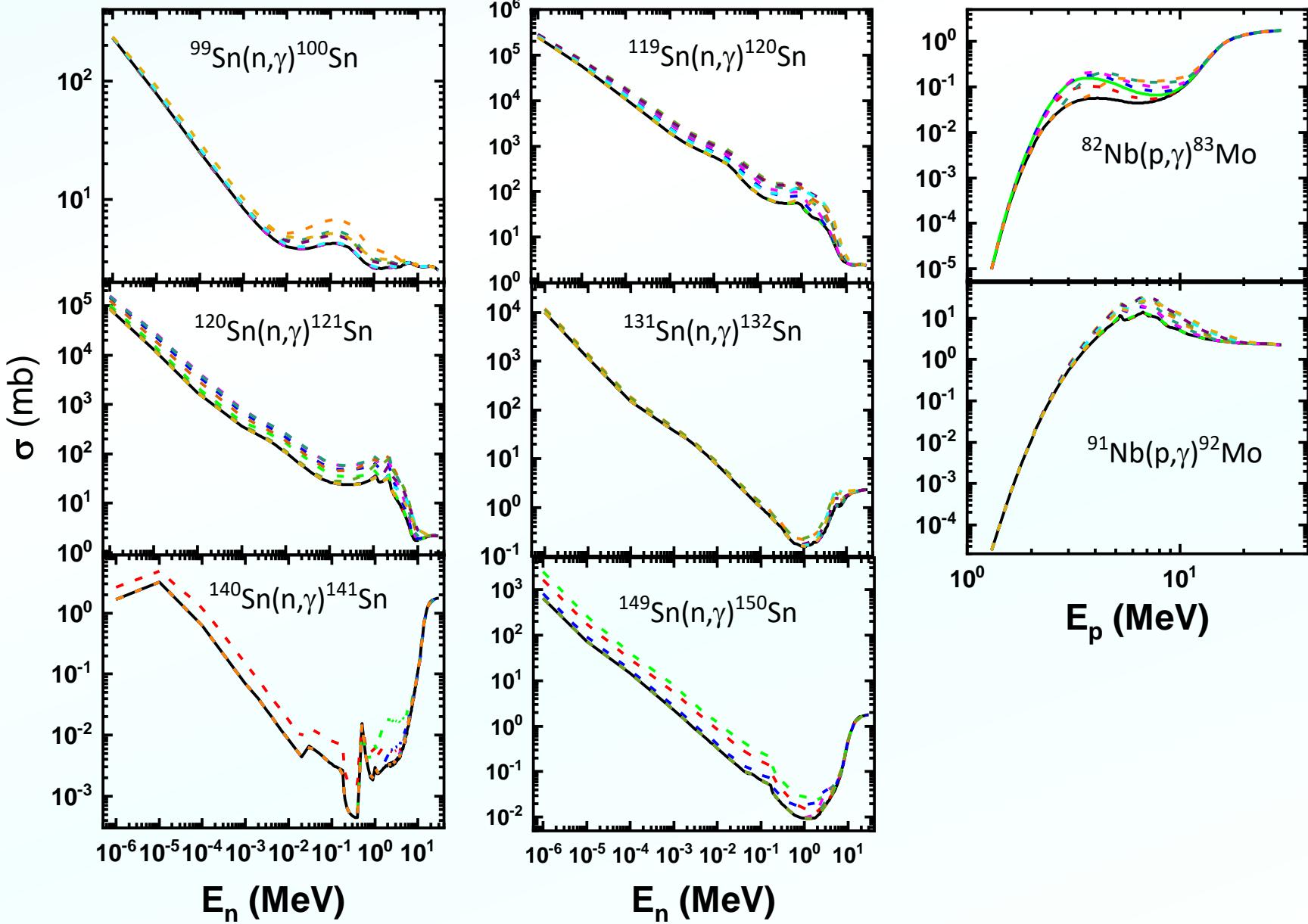
✓ Procedure

- microscopic HFB + comb. method
- successively scale the energy range of NLD by 10 within an energy interval of $\Delta E = 1$ MeV from 0 up to proton or neutron separation energy for both positive and negative parities simultaneously

$$\Omega_{S_q} = \frac{\nu_{\Omega} - 1}{\nu_q - 1}$$

↳ 10

STEP I



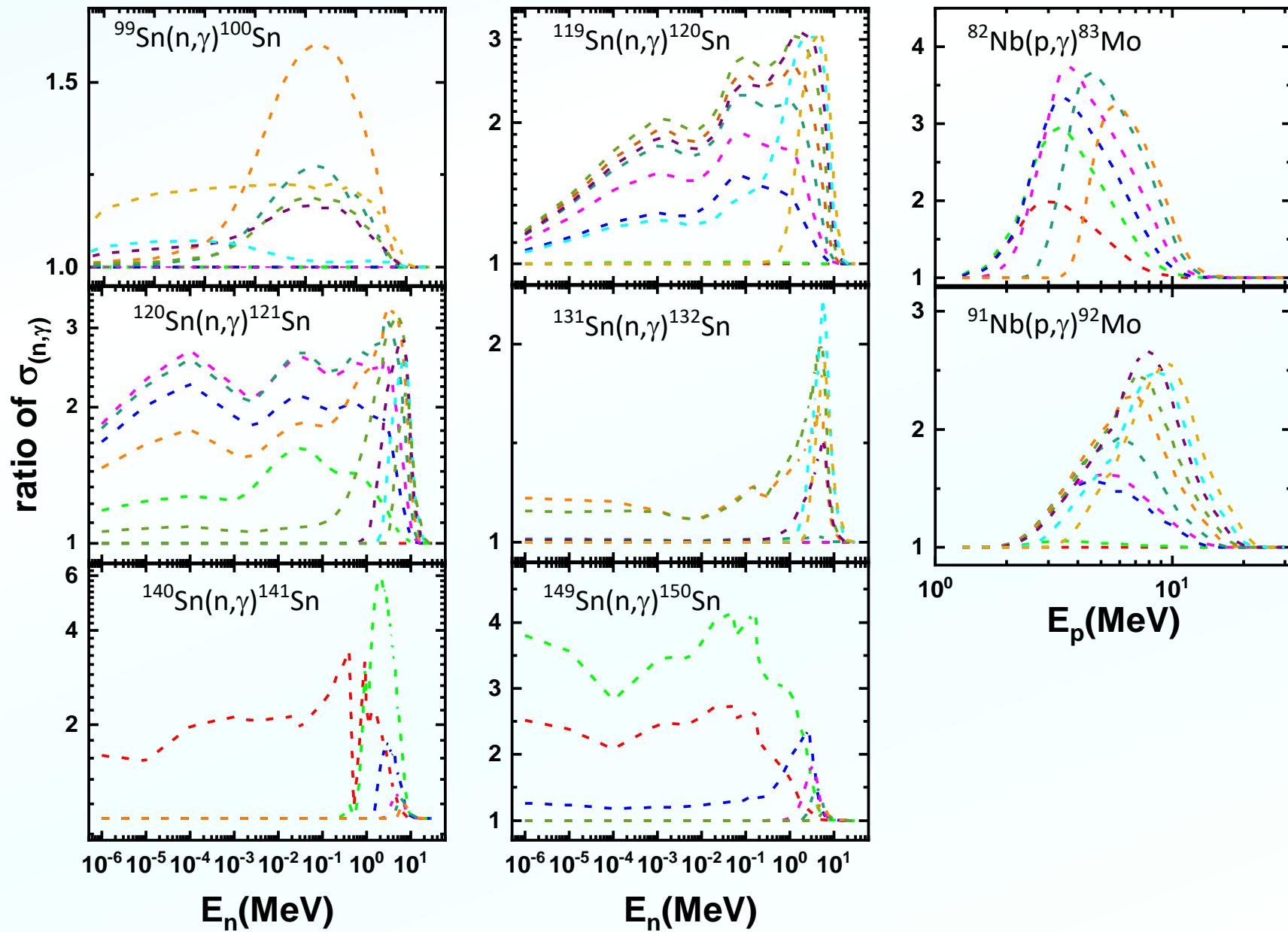
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STEP II



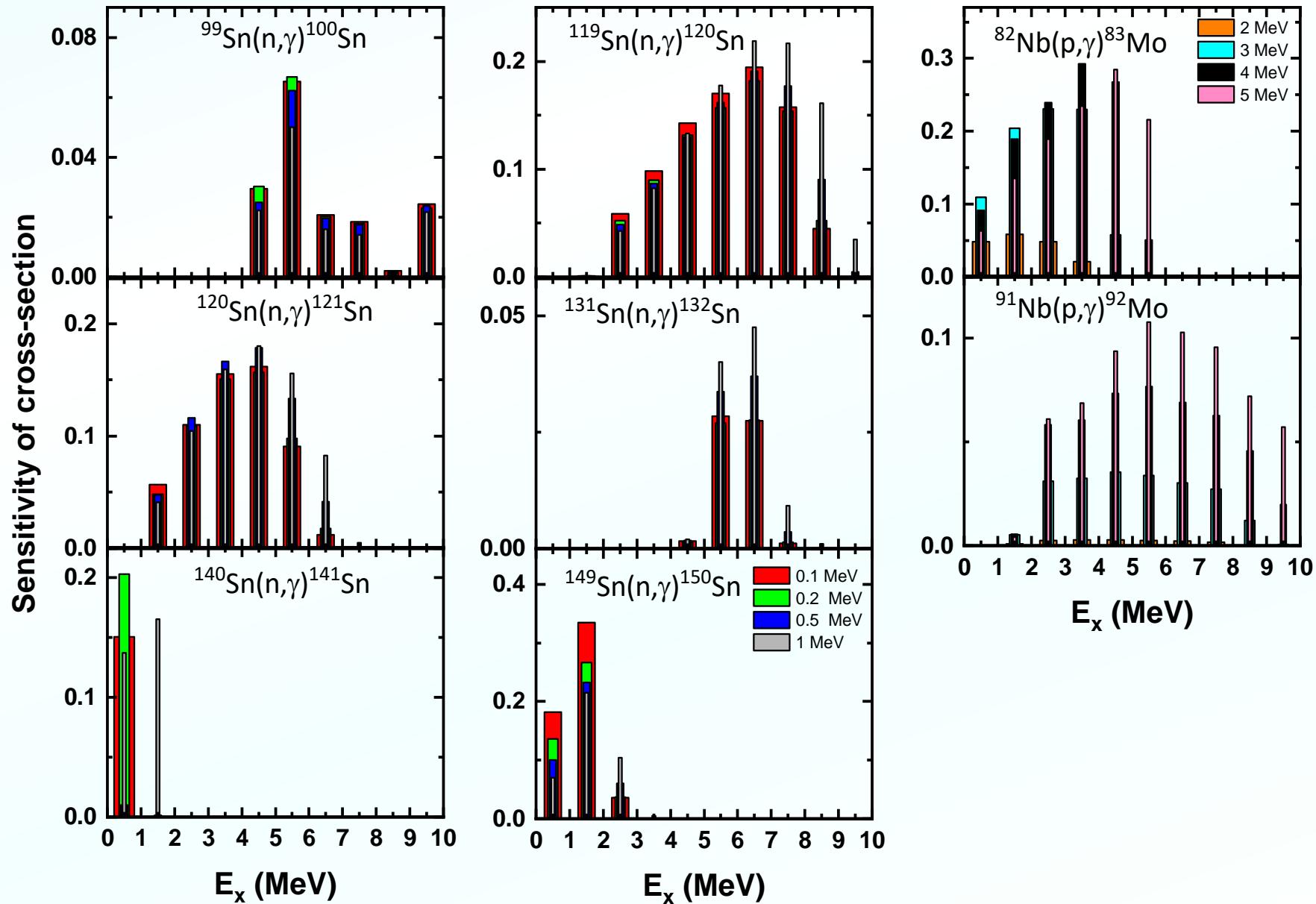
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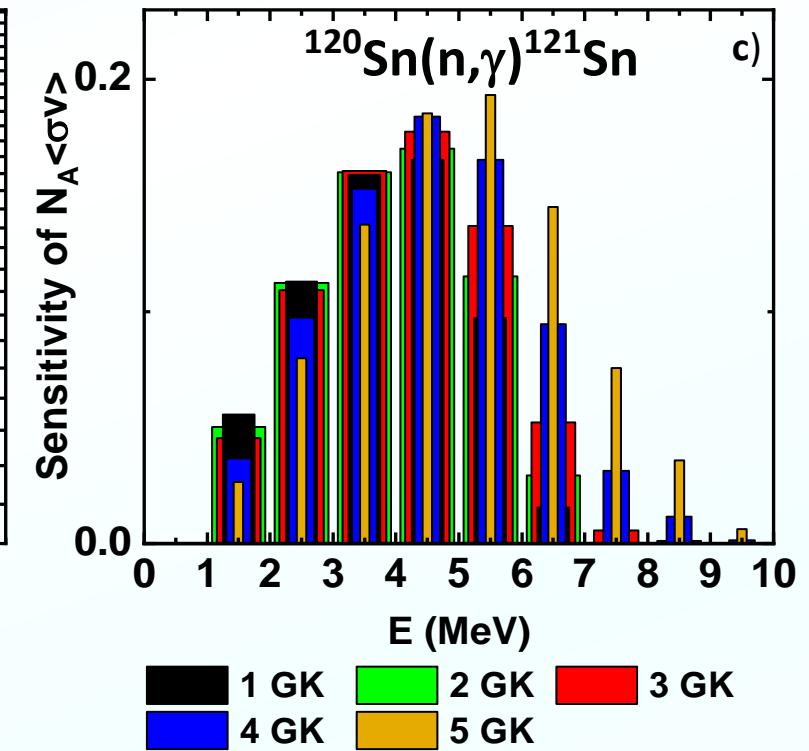
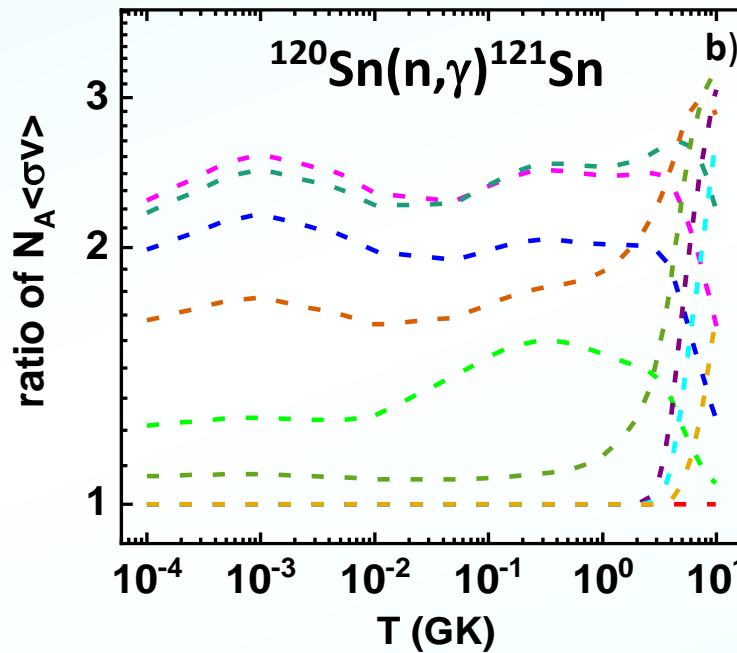
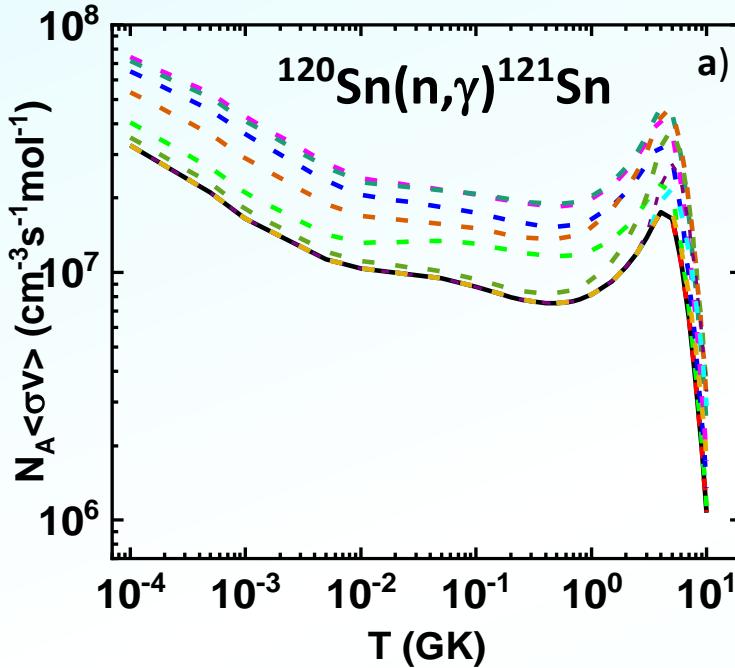
$$\Omega_{S_q} = \frac{\nu_{\Omega} - 1}{\nu_q - 1}$$

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STEP III



Sensitivity of the astrophysical reaction rate

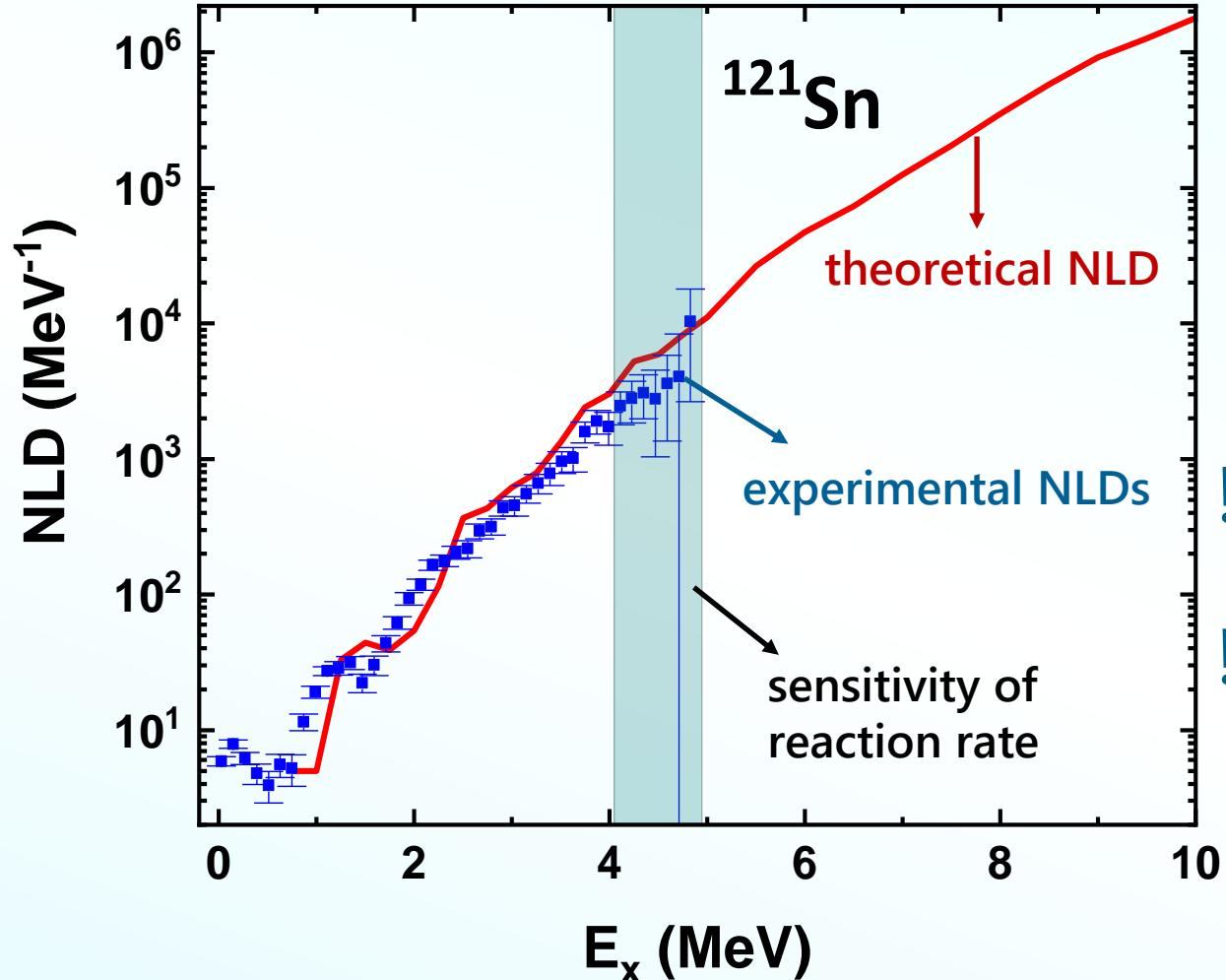


✓ observable differences between the data

✓ these ratios can reach values up to 3 within 1 - 10 MeV

✓ $T = 1 - 4\text{ GK}$: the sensitivity is confined to [4,5] MeV
✓ $T = 5\text{ GK}$: the sensitivity predominates in [5,6] MeV

Even with an enhancement of the NLD energy by a factor of 10, the reaction rate sensitivity consistently remains within the 4 - 5 MeV



- ✓ the theoretical NLD is compared to the NLD measured by the Oslo method
 - ↓
 - significant uncertainties
 - { minimize these uncertainties
 - enhance the reliability and accuracy
- ! could provide critical insights to nuclear reaction models
- ! could guide experimental measurements, particularly those targeting level schemes at the excitation energies of 4 - 5 MeV

To be submitted to Physica Scripta

Take home messages

The present study examines the sensitivity of reaction cross-section and astrophysical reaction rate to NLD across different energy intervals

❖ nucleon capture cross-sections

- ✓ stable nuclei contribute to nucleon capture cross-sections across a broader energy range
- ✓ rich nuclei exhibit contributions concentrated within narrower energy intervals

❖ astrophysical reaction rate

4 - 5 MeV range is the critical energy interval with the most significant impact on reaction rate calculation

Thank you!